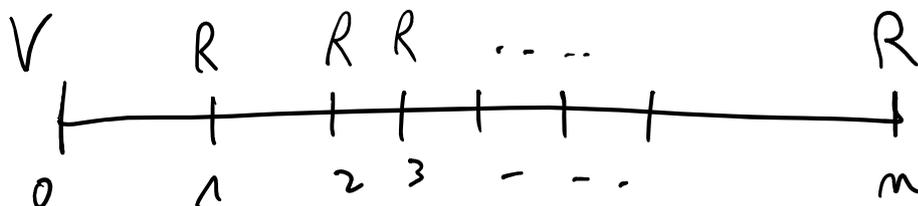


Suggerimento per corso a scelta terzo anno:
Modelli e Metodi per l'Economia e la Finanza



$$V = R \cdot \frac{1}{1+i} + R \cdot \frac{1}{(1+i)^2} + R \cdot \frac{1}{(1+i)^3} + \dots + R \cdot \frac{1}{(1+i)^m}$$

$$V = R \cdot q + R \cdot q^2 + R \cdot q^3 + \dots + R \cdot q^m$$

$$Vq = R \cdot q^2 + R \cdot q^3 + R \cdot q^4 + \dots + R \cdot q^{m+1}$$

SOTTRAZIONE

$$\underbrace{V}_{\sim} - \underbrace{Vq}_{\sim} = \underbrace{Rq}_{\sim} - \cancel{Rq^2} + \cancel{Rq^2} - \cancel{Rq^3} + \cancel{Rq^3} - \cancel{Rq^4} + \dots + \cancel{Rq^m} - \underbrace{Rq^{m+1}}_{\sim}$$

$$V - Vq = Rq - Rq^{m+1}$$

$$V(1-q) = Rq \cdot (1-q^m)$$

$$V = Rq \cdot \frac{1-q^m}{1-q}$$

$$q = \frac{1}{1+i}$$

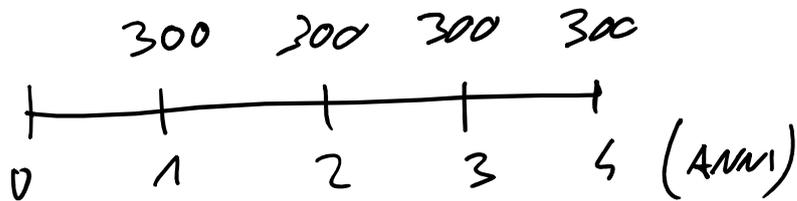
$$v = \frac{1}{1+i} = \frac{1}{1+i}$$

$$q = \frac{1}{1+i}$$

$$V = R \cdot \frac{1}{1+i} \cdot \frac{1 - \left(\frac{1}{1+i}\right)^m}{1 - \frac{1}{1+i}}$$

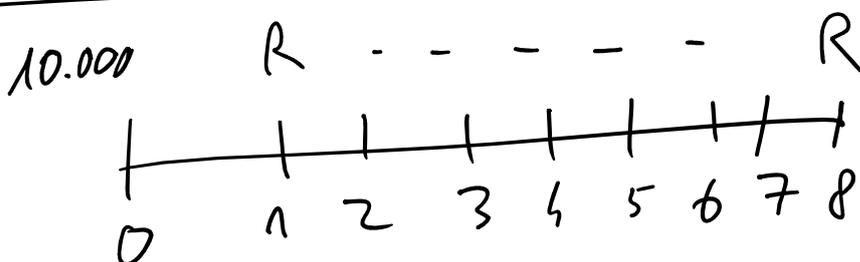
$$V = R \cdot \frac{1}{1+i} \cdot \frac{1 - (1+i)^{-m}}{\frac{1+i-1}{1+i}}$$

$$V = R \cdot \frac{1 - (1+i)^{-m}}{i}$$



$i = 5\%$ ANNUO $? = V$

$$V = 300 \cdot \frac{1 - (1 + 0.05)^{-4}}{0.05}$$



0 1 2 3 4 5 6 7 8

$i = 3\%$ $n = 8$ $R = ?$

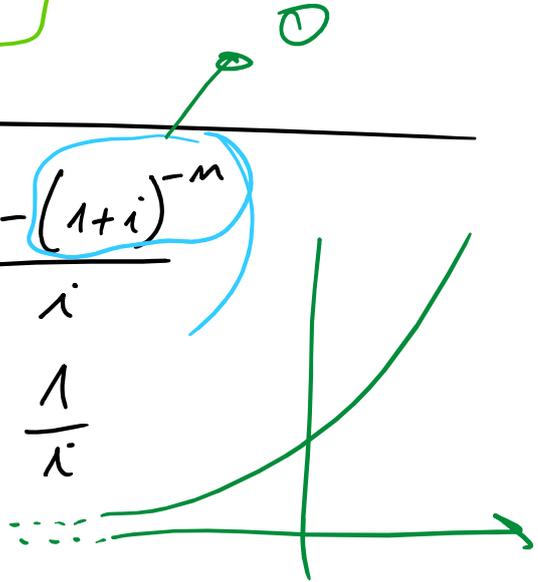
$$10.000 = R \cdot \frac{1 - (1 + 0.03)^{-8}}{0.03}$$

POST. TEMP

$$V \stackrel{li}{=} R \cdot \frac{1 - (1+i)^{-n}}{i}$$

POST ILLIMITATA

$$V = R \cdot \frac{1}{i}$$



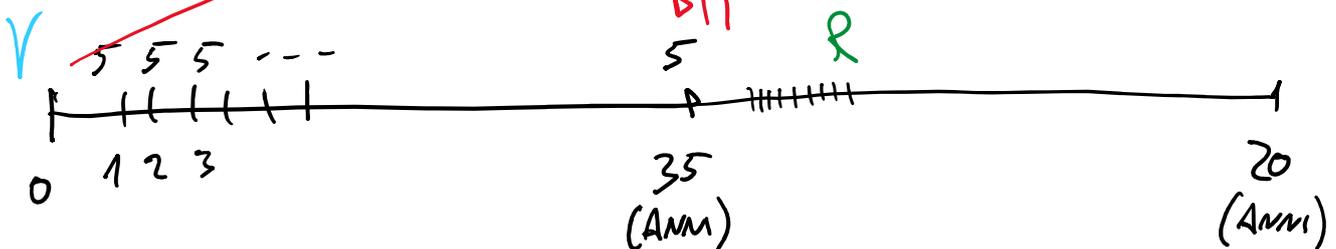
TIZIO VERSA 5000€/ANNO

POSTICIPATI PER 35 ANNI

SE TI ASPETTO DI VIVERE 20 ANNI

IN PENSIONE, QUAL'È LA PENSIONE TRUSSIERA (POSTICIPATA)?

$i = 2\%$ ANNO



$$V = \dots \frac{1 - (1 + 0.02)^{-35}}{0.02}$$

$$V = 5000 \cdot \frac{1 - (1 + 0.02)^{-35}}{0.02} = 126993 \text{ €}$$

$$\Pi = 126993 \cdot (1 + 0.02)^{35} = 249972 \text{ €}$$

$$249972 = R \cdot \frac{1 - (1 + 0.001652)^{-240}}{0.001652}$$

$$R = 1262 \text{ €}$$

$$(1 + 0.02)^1 = (1 + i^*)^{12}$$

$$i^* = \sqrt[12]{1.02^1} - 1 = 0,1652\%$$