

Mathcad (chaotic?) trajectories

1

We show how to let Mathcad construct trajectories for a scalar discrete-time dynamic system.

The motion law $x(t+1) = f[x(t)]$ can be chosen *ad libitum*. The function f is nothing but evolution one. In this worksheet we focus on the case of a logistic model. Two parameters are needed:

parameters

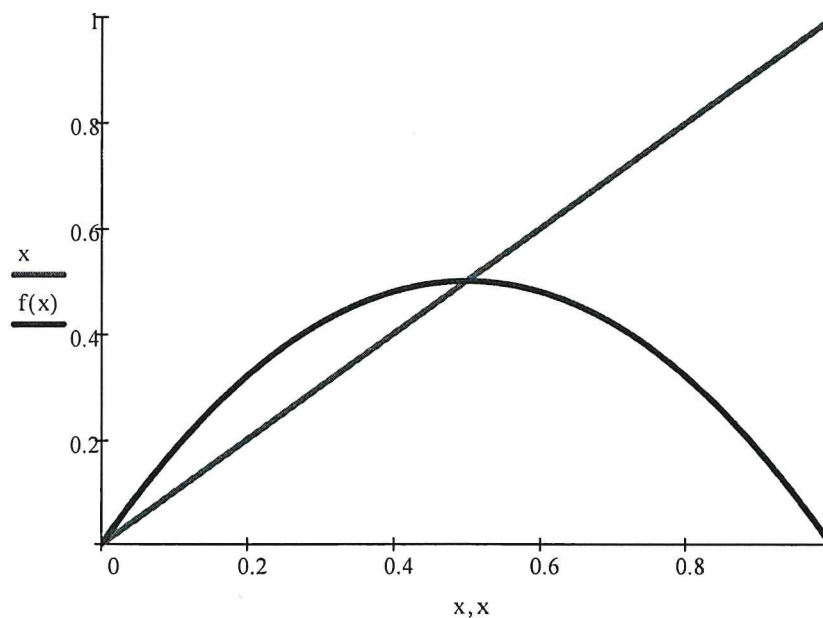
$$a := 2$$

$$M := 1$$

recommended values, in order to understand are $a = 2, 3, 4$. I encourage studs in making experiments.

evolution function:

$$f(x) := a \cdot x \cdot (M - x)$$



MACHINERY FOR THE CONSTRUCTION OF THE TRAJECTORY

$$T := 10 \quad \text{Half the time horizon}$$

$$t := 1..2 \cdot T$$

$$s_w := 1..T$$

$$tt := 0..2 \cdot T$$

$$X_0 := .1 \qquad Y_0 := f(X_0) \qquad Y_0 = 0.18$$

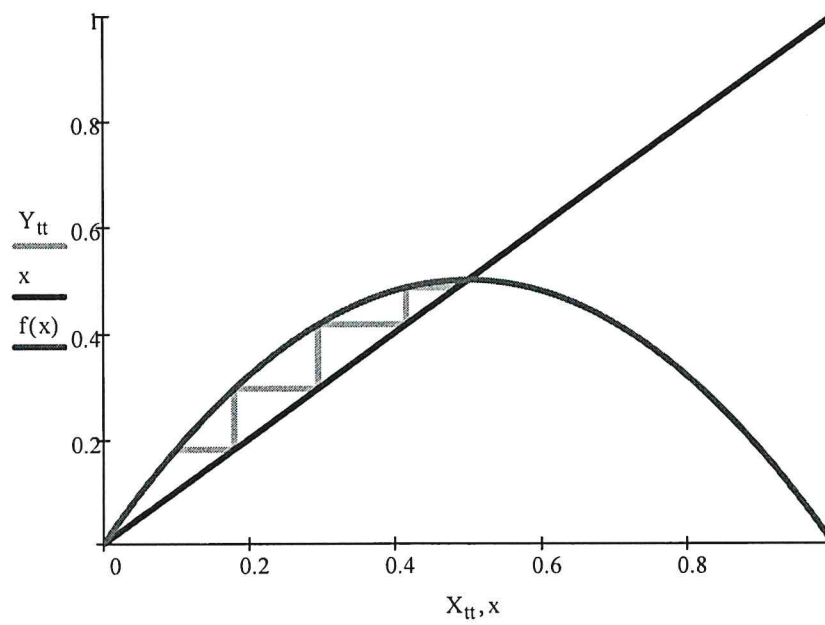
$$X_{2 \cdot s} := f[X_{2 \cdot (s-1)}]$$

$$Y_{2 \cdot s} := f(X_{2 \cdot s})$$

$$X_{2 \cdot s-1} := Y_{2 \cdot (s-1)}$$

$$Y_{2 \cdot s-1} := Y_{2 \cdot (s-1)}$$

END OF THE MACHINERY



$$x_0 := X_0 \qquad x_0 = 0.1$$

$$t := 1..2 \cdot T$$

$$x_t := f(x_{t-1})$$

